

Questions can be answered in multiple ways. Both ways must be known for mastery

Energy vs. Force Net

A 0.25kg rock is thrown up at 20m/s.
 How high will the rock travel?
 How fast is the rock at 10m high?

Kinematics

$$V_f = V_i + at$$

$$0 = 20 + (-9.8)t$$

$$\frac{-20}{-9.8} = t$$

$$t = 2.04 \text{ s}$$

$$y_t = y_0 + V_i t + \frac{1}{2} a t^2$$

$$= 0 + 20(2.04) + \frac{1}{2}(-9.8)(2.04)^2$$

$$40 + 19.6$$

$$y_t = \boxed{20.4 \text{ m}}$$

energy

$$KE = mhg$$

$$\frac{1}{2} m v^2 = mhg$$

$$\frac{v^2}{2g} = h$$

$$\frac{v^2}{2g} = h$$

$$\frac{20^2}{2 \cdot 10} = \boxed{20 \text{ m}}$$

A rocket with a mass of 2.5kg launches up to a height of 800m in 3 seconds.

(motor burns out after 3 sec)

What is the force of the engine?

How fast is the rocket traveling at 800m?

How much higher will the rocket go up before stopping?

$$x_t = x_i + v_i t + \frac{1}{2} a t^2$$

$$800 = 0 + 0 + \frac{1}{2} a (3)^2$$

$$a = 177.7 \text{ m/s}^2$$

$$V_f = V_i + at$$

$$= 0 + 177(3)$$

$$V_f = \boxed{533 \text{ m/s}}$$

$$V_f = V_i + at$$

$$0 = 533 + (-9.8)t$$

$$t = 54.48 \text{ s}$$

$$V_f^2 = V_i^2 + 2ad$$

$$\frac{v^2}{2a} = d$$

high
14204m

Energy

@800m
 $V = 533 \text{ m/s}$
 total energy of Rocket

$$KE + PE =$$

$$\frac{1}{2} (2.5) 533^2 + 2.5(10) 800$$

$$355111 \text{ J} + 20000 \text{ J}$$

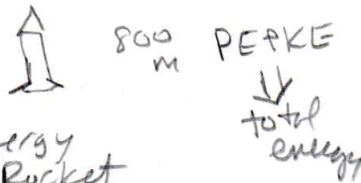
$$= 375111 \text{ J}$$

Height using Energy

$$ENERGY = PE$$

$$375111 = mhg$$

$$h = \boxed{15000 \text{ m}}$$



$$F \cdot d = \text{Energy}$$

$$F_{\text{ave}} = \frac{\text{Energy}}{d}$$

$$\boxed{468 \text{ N}} = \frac{375111}{800}$$

Except

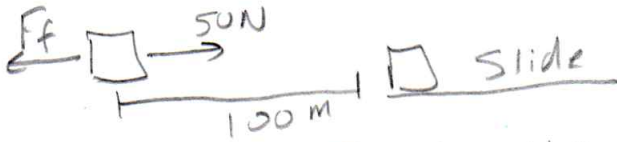
A 20kg Box is dragged with a 50N force for 100m then allowed to slide with no force added.

The $\mu_k = 0.2$.

How fast will the box be traveling at 100m?

How much energy is the person exerting?

How far will the box slide if allowed to slide after the 100m mark.



$$a = \frac{\Sigma F}{m} \quad \frac{F_a - F_f}{m} = \frac{50 - 40}{20} = 0.5$$

$$F_f = F_n \cdot \mu$$

$$20 \cdot 10 \cdot 0.2 = 40 \text{ N} = F_f$$

$$x_t = x_i + v_i t + \frac{1}{2} a t^2$$

$$0 = 0 + 0 + \frac{1}{2} (0.5) t^2$$

$$t = 20 \text{ sec.}$$

$$v_f = v_i + a t$$

$$= 0 + 0.5 \cdot (20)$$

$$\boxed{10 \text{ m/s}} @ 100 \text{ m}$$

Energy

$$\text{Energy} = F \cdot d$$

$$50 \cdot 100 = 5000 \text{ J}$$

$$5000 = \text{KE} + \text{TE} \quad \text{Friction}$$

$$5000 = \frac{1}{2} m v^2 + m g u d$$

$$\frac{1}{2} (20) v^2 + 20 \cdot 10 \cdot 0.2 \cdot 100$$

$$10 v^2 = 4000 \text{ J}$$

$$\sqrt{\frac{10000}{10}} = 10 \text{ v}^2$$

$$10 = v$$

same

Let go of Rope

$$a = \frac{\Sigma F}{m} = \frac{F_f}{m} = \frac{-40}{20} = -2 \text{ m/s}^2$$

$$v_t = v_i + a t$$

$$= 10 + -2(t) \quad t = 5 \text{ sec}$$

$$x_t = x_i + v_i t + \frac{1}{2} a t^2$$

$$= 0 + 10(5) + \frac{1}{2} (-2)(5)^2$$

$$50 + -25$$

$$\boxed{x_t = 25 \text{ m}}$$

further
(125 total)

How much further will it slide

$$\text{KE} \rightarrow \text{TE} \quad \text{friction}$$

$$\frac{1}{2} m v^2 = m g u d$$

$$\frac{v^2}{2 g u} = d$$

$$\frac{10^2}{2 \cdot 10 \cdot 0.2} = \boxed{25 \text{ m}}$$